Please write Your name:

You may leave your answer in terms of sums, products, factorials or binomial coefficients, and fractions. There is NO need to simplify. NO calculators are needed.

.....

Suppose X has the following p.d.f.

$$f(x) = \begin{cases} a(x-1) & \text{if } 1 \leq x \leq 3\\ 0 & \text{otherwise} \end{cases}$$

(1) Find a

(2) Find $\mathbb{P}(X \leq 2)$

Suppose X has the following p.d.f.

$$f(x) = \begin{cases} \frac{1}{4} & \text{if } -2 \leqslant x \leqslant 2\\ 0 & \text{otherwise} \end{cases}$$

(3) Find $\mathbb{E}X$

(4) Find Var(X)

2

Suppose X has the following p.d.f.

$$f(x) = \begin{cases} \frac{1}{x^2} & \text{if } x \ge 1\\ 0 & \text{otherwise} \end{cases}$$

(5) Find $\mathbb{P}(X \leq 3)$

(6) Can you find $\mathbb{E}X$? Explain your answer.