Please write Your name:

Show all work. You should either write at a sentence explaining your reasoning, or annotate your math work with brief explanations. There is no need to simplify, and no calculators are needed. One two sided page of handwritten notes is allowed.

(1a) A password must contain exactly 1 capital letter, 3 lowercase letters, and 3 digits. Characters can be repeated, and the order matters. How many different 7-character passwords are possible?

(1b) Answer the same question if all the characters must be different. Here B and b are considered different characters.

(2d)	What	is t	the su	ım of	the	prob	abili [.]	ties i	n qu	estion	s (2a)	, (2b)	and	(2c)?	Explain
(2e)	What	is t	the pr	obab	oility	that	if w	e roll	l 3 d	ice, th	e sum	is 5?			

Suppose that X is a random variable with the outcomes $\{0, 1, 2, 3\}$. The corresponding probabilities are given by

$$\mathbb{P}(X=0) = \frac{1}{3}, \qquad \mathbb{P}(X=1) = \frac{1}{6}, \qquad \mathbb{P}(X=2) = \frac{1}{6}, \qquad \mathbb{P}(X=3) = \frac{1}{3}$$

(3a) Make a picture for the probability mass function. Indicate on this picture the location of $\mathbb{E}X$

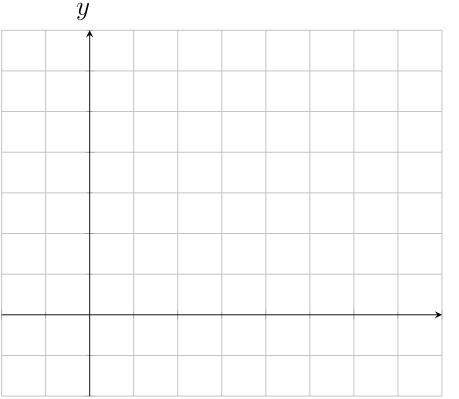
(3b) Compute $\mathbb{E}X$.

(3c) Does your answer for $\mathbb{E}X$ agree with your picture above?

(3d) Find Var(X) but do not simplify.

(3e) Find the cumulative distribution function F_X of X using the cases provided below.

(3f) Plot the cumulative distribution function F_X of X using the chart provided below. Accurately label values at x and y axes.



 \mathcal{X}

$[(optional\ questions\ for\ extra\ credit)]:$
You roll a dice 4 times and win \$1 for every even number rolled, and \$2 for every odd number rolled. What is the probability that you win \$7 or more?
What is the expected number of dollars that you win if you play this game?
y a real real real real real real real re
What is the standard deviation of the number of dollars that you win if you play this game?