

Please write **Your name:** \_\_\_\_\_

**Show all work:** either write at least a sentence explaining your reasoning, or annotate your math work with brief explanations. Correct answer with no solution will give only a partial credit. There is NO need to simplify, and NO calculators are allowed. You may leave your answer in terms of sums, products, powers, factorials or binomial coefficients, and fractions.

(1a) If we perform **10** independent experiments, and each experiment has probability of success **0.1**, what is the probability that at least **2** of them are successful?

**Answer:**

$$\mathbb{P}(X \geq 2) = 1 - (9/10)^{10} - (9/10)^9 \approx 0.2639$$

(1b) What is the Poisson approximation to the same probability?

**Answer:**

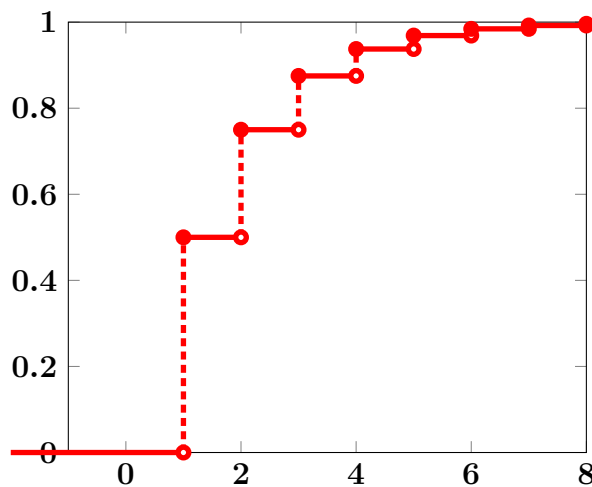
$$\mathbb{P}(X \geq 2) \approx 1 - 2e^{-1} \approx 0.2642$$

2(a) If  $X$  is a Geometric random variable with  $p = \frac{1}{2}$ , find  $\mathbb{P}(X \geq 2 | X \geq 1)$ .

**Answer:**  $\mathbb{P}(X \geq 2 | X \geq 1) = 1/2$

(2b) Plot the cumulative distribution function  $F_X$  of  $X$  using the chart provided below. Accurately label values at  $x$  and  $y$  axes.

**Answer:**



end of the quiz